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4.

$$f(x) = 2x^3 - \frac{7}{x^2} + 16, \quad x \neq 0$$

The equation $f(x) = 0$ has a single root α between $x = -2$ and $x = -1$

(a) Starting with the interval $[-2, -1]$, use interval bisection twice to find an interval of width 0.25 that contains α.

(3)

The equation $f(x) = 0$ also has a single root β in the interval $[0.6, 0.7]$.

(b) Taking 0.65 as a first approximation to β, apply the Newton-Raphson procedure once to $f(x)$ to obtain a second approximation to β, giving your answer to 4 decimal places.

(4)

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Question 4 continued

Q4

(Total 7 marks)