3. The hyperbola H has equation $xy = c^2$ where c is a positive constant.

The point $P\left(ct, \frac{c}{t}\right)$, where $t > 0$, lies on H.

The tangent to H at P meets the x-axis at the point A and meets the y-axis at the point B.

(a) Determine, in terms of c and t,

(i) the coordinates of A,

(ii) the coordinates of B.

(4)

Given that the area of triangle AOB, where O is the origin, is 90 square units,

(b) determine the value of c, giving your answer as a simplified surd.

(2)

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Question 3 continued

(Total for Question 3 is 6 marks)