6. (i)

$$f(x) = x - 4 - \cos\left(5\sqrt{x}\right) \qquad x > 0$$

(a) Show that the equation $f(x) = 0$ has a root α in the interval [2.5, 3.5]

(2)

(b) Use linear interpolation once on the interval [2.5, 3.5] to find an approximation to α, giving your answer to 2 decimal places.

(2)

(ii)

$$g(x) = \frac{1}{10}x^2 - \frac{1}{2x^2} + x - 11 \qquad x > 0$$

(a) Determine $g'(x)$.

(2)

The equation $g(x) = 0$ has a root β in the interval [6, 7]

(b) Using $x_0 = 6$ as a first approximation to β, apply the Newton–Raphson procedure once to $g(x)$ to find a second approximation to β, giving your answer to 3 decimal places.

(2)

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Question 6 continued

(Total for Question 6 is 8 marks)