8. (a) Use the standard results for summations to show that, for all positive integers n,

$$\sum_{r=1}^{n} r\left(2r^2 - 3r - 1\right) = \frac{1}{2}n(n+1)^2(n-2)$$

(4)

(b) Hence show that, for all positive integers n,

$$\sum_{r=n}^{2n} r\left(2r^2 - 3r - 1\right) = \frac{1}{2}n(n-1)(an+b)(cn+d)$$

where a, b, c and d are integers to be determined.

(4)

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